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CONTENTS

1	Linear Combination	1
2	Differentiation and Integration	2
3	Practical Verification	2

Abstract—This manual shows how to use an OPAMP for implementing mathematical functions.

1 LINEAR COMBINATION

Problem 1. In Fig. 1, the current entering the + and – terminals of the opamp is 0. The voltages at both terminals is v . Show that

$$y = k_1 x_1 - k_2 x_2, \quad k_1, k_2 > 0 \quad (1)$$

where x_1, x_2 are the inputs. Find the values of k_1 and k_2 .

Solution: Using node analysis,

$$\frac{v - x_2}{R_2} + \frac{v - y}{R_f} = 0 \quad (2)$$

$$\frac{v - x_1}{R_1} + \frac{v}{R_3} = 0 \quad (3)$$

resulting in

$$v \left(\frac{1}{R_2} + \frac{1}{R_f} \right) = \frac{x_2}{R_2} + \frac{y}{R_f} \quad (4)$$

$$\frac{x_1}{R_1} = v \left(\frac{1}{R_1} + \frac{1}{R_3} \right) \quad (5)$$

Simplifying,

$$1 \quad \frac{x_1}{R_1} \left(\frac{1}{R_2} + \frac{1}{R_f} \right) = \frac{x_2}{R_2} \left(\frac{1}{R_1} + \frac{1}{R_3} \right) + \frac{y}{R_f} \left(\frac{1}{R_1} + \frac{1}{R_3} \right) \quad (6)$$

$$\Rightarrow y = \frac{-\frac{x_2}{R_2} \left(\frac{1}{R_1} + \frac{1}{R_3} \right) + \frac{x_1}{R_1} \left(\frac{1}{R_2} + \frac{1}{R_f} \right)}{\frac{1}{R_f} \left(\frac{1}{R_1} + \frac{1}{R_3} \right)} \quad (7)$$

$$= \underbrace{\frac{R_3 (R_2 + R_f)}{R_1 (R_1 + R_3)}}_{k_1} x_1 - \underbrace{\frac{R_f}{R_2}}_{k_2} x_2 \quad (8)$$

$$= k_1 x_1 - k_2 x_2 \quad (9)$$

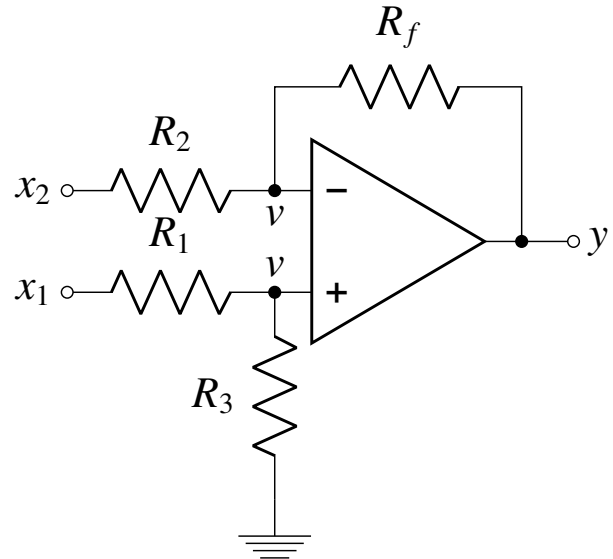


Fig. 1: $y = k_1 x_1 - k_2 x_2$.

Problem 2. Design a circuit for

$$y = kx, \quad k > 0 \quad (10)$$

Problem 3. Design a circuit for

$$y = -kx, \quad k > 0 \quad (11)$$

2 DIFFERENTIATION AND INTEGRATION

Problem 4. Design a circuit for

$$x = -k \frac{dy}{dt}, k > 0 \quad (12)$$

and obtain an expression for k .

Solution: Fig. 2 provides the solution which is explained below. Using node analysis in the s domain,

$$\frac{V(s) - Y(s)}{R} + sCV(s) - X(s) = 0 \quad (13)$$

Since $v = 0$, the above equation results in

$$Y(s) = -sCRX(s) \quad (14)$$

$$\Rightarrow y(t) = - \underbrace{RC}_k \frac{dx}{dt} \quad (15)$$

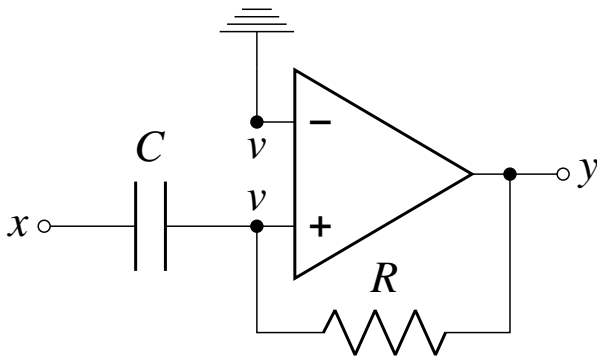


Fig. 2: $y = -k \frac{dx}{dt}$.

Problem 5. Modify the circuit in Problem 4 to obtain

$$y = k \int x(t) dt \quad (16)$$

Is $k > 0$?

Problem 6. How will you obtain

$$y = k \frac{dx}{dt}, \quad k > 0? \quad (17)$$

3 PRACTICAL VERIFICATION

In the following, $1k\Omega$ and $2k\Omega$ resistances are available.

Problem 7. Verify your circuit in Problem 1 for $x_1 = 0.5V, x_2 = 1V, y = -1.1.V$.

Problem 8. Verify your circuit for (10) for $x = 0.5V$ and $y = 1.5V$. You will have to choose the resistances appropriately.

Problem 9. Verify your circuit for (11) if $x = 1V, y = -2V$.

Problem 10. A triangular wave with $V_{pp} = 1V$ and frequency 100 Hz is given as the input in Problem 4. What is the output for $C = 1\mu F$ and $R = 10k\Omega$? Verify your result.