Python for Signals and Systems

Prashant Kumar Aleshwaram†, Mohammed Zafar Ali Khan* and G V V Sharma*

***Abstract*—This manual provides an introduction to signals and systems through simple python scripts.**

Problems 1-5 are related.

Problem 1. Let

$$x(n) = \left\{ \underset{\uparrow}{0}, 2, 3, 1 \right\} \tag{1.1}$$

Sketch $x(n)$

Solution: The following code yields Fig. 1.

```
import numpy as np
import matplotlib.pyplot as plt

n=np.linspace(-3,7,11)
x=np.array
    ([0,0,0,0,2,3,1,0,0,0,0])
plt.stem(n,x)
plt.xlabel('$n$')
plt.ylabel('$x(n)$')
plt.ylim((0,3))
#Ignore the following command
plt.savefig('../figs/3a.eps')
plt.show()
```

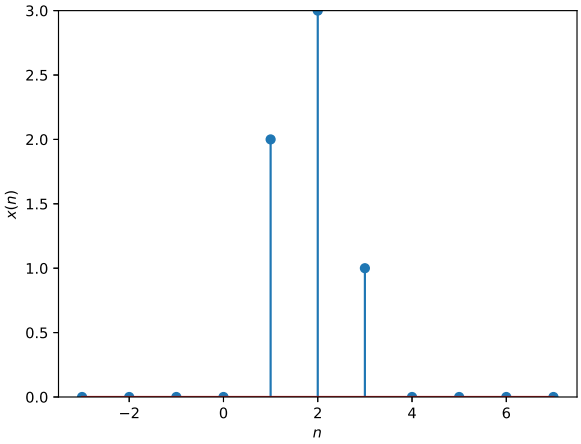

Fig. 1

Problem 2. Is $x(n)$

1) An energy signal?
2) A power signal?
3) A causal signal?
4) A periodic signal?

Problem 3. Sketch $3x(n)$.

Solution: The following code yields Fig. 3.

```
import numpy as np
import matplotlib.pyplot as plt

n=np.linspace(-3,7,11)
x=np.array
    ([0,0,0,0,2,3,1,0,0,0,0])
plt.stem(n,3*x)
plt.xlabel('$n$')
plt.ylabel('$3x(n)$')
plt.ylim((0,10))
#Ignore the following command
plt.savefig('../figs/3b.eps')
plt.show()
```

Problem 4. Sketch $x(n-2)$.

Solution: The following code yields Fig. 4.

```
import numpy as np
import matplotlib.pyplot as plt
from scipy.ndimage.interpolation
    import shift
```

*The authors are with the Department of Electrical Engineering, Indian Institute of Technology, Hyderabad 502285 India e-mail: {zafar,gadepall}@iith.ac.in.† The author is an intern with the Teaching Learning Centre, IIT Hyderabad email: akumar10@student.nitw.ac.in.

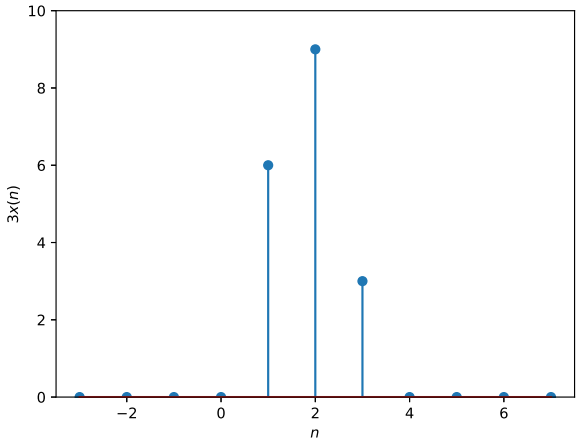

Fig. 3

```
n=np.linspace(-3,7,11)
#x(n)
xn=np.array
    ([0,0,0,2,3,1,0,0,0,0])
#x(n-2)
xn_right=shift(xn, 2, cval=0)

plt.stem(n,xn_right)
plt.xlabel('$n$')
plt.ylabel('$x(n-2)$')
plt.ylim((0,4))
#Ignore the following command
plt.savefig('../figs/3c.eps')
plt.show()
```

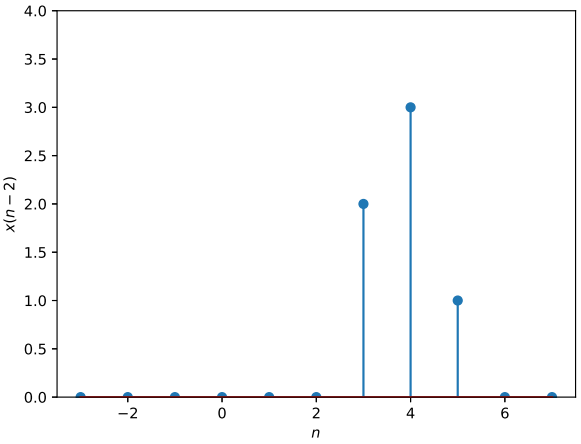

Fig. 4

Problem 5. Sketch $x(3-n)$.

Solution: The following code yields Fig. 5.

```
import numpy as np
import matplotlib.pyplot as plt
from scipy.ndimage.interpolation
    import shift


#x(n)
xn=np.array([0,0,0,2,3,1])
#x(-n)
xflip = np.flip(xn,0)
#x(3-n)
xflip_right=shift(xflip, 3, cval
    =0)
#plotting
n=np.linspace(-3,3,7)
plt.stem(n, xflip_right)
plt.xlabel('$n$')
plt.ylabel('$x(3-n)$')
plt.ylim((0,4))
##Ignore the following command
plt.savefig('../figs/3d.eps')
plt.show()
```

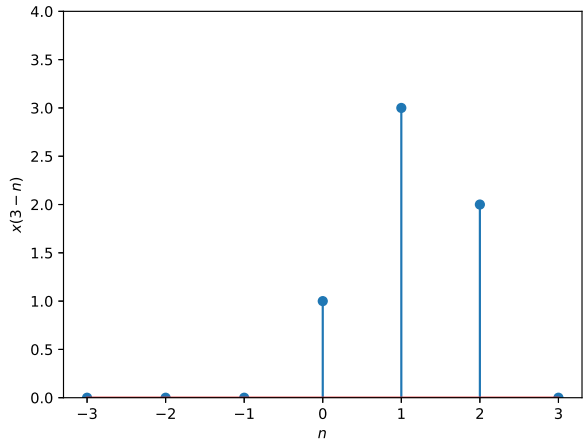

Fig. 5

Problem 6. Sketch

$$x(t) = \begin{cases} 4 - |t| & 1 \le |t| \le 4 \\ 2 + |t| & |t| < 1 \end{cases} \tag{6.1}$$

and find out if its even or odd.

Solution: The following code yields Fig. 6. As we can see, $x(t) = x(-t)$ and the function is even.

```
import numpy as np
import matplotlib.pyplot as plt

#|t| < 1
t1=np.linspace(-1,1,25)
x1=2+abs(t1)

#1 < |t| < 4
t2=np.linspace(1,4,25)
x2=-abs(t2)+4
t3=np.linspace(-4,-1,25)
x3=(t3)+4

#x(t)
x=np.concatenate((x3,x1,x2), axis
    = 0)

t = np.concatenate((t3,t1,t2),
    axis = 0)

#x(-t)
xflip = np.fliplr([x])[0]


#Plotting
plt.plot(t,x, label='$x(t)$')
plt.plot(t,xflip,'o', mfc='none',
    label='$x(-t)$')

plt.grid()
plt.xlabel('$t$')
plt.ylabel('$x(t)$')
plt.legend()
##Ignore the following command
plt.savefig('../figs/4a.eps')
plt.show()
```

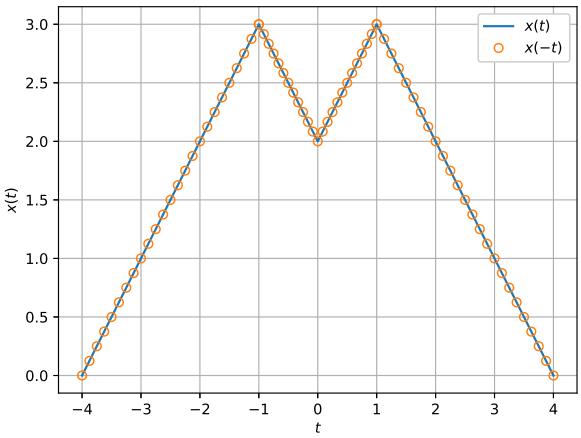

Fig. 6

Problem 7. Sketch

$$x(t) = \begin{cases} t+4 & -4 \le t \le -1 \\ -5t-2 & -1 < t < 0 \\ \frac{2}{3}(t-3) & 0 \le t \le 3 \\ 0 & \text{otherwise} \end{cases} \tag{7.1}$$

and find out if its even or odd.

Solution: The following code yields Fig. 7. As we can see, the function is neither even nor odd.

```
import numpy as np
import matplotlib.pyplot as plt

#-4 < t <-1
t3=np.linspace(-4,-1,60)
x3=t3+4

#-1 < t < 0
t1=np.linspace(-1,0,20)
x1=-5*t1-2

#0 < t < 3
t2=np.linspace(0,3,60)
x2=(2.0/3)*(t2-3)

#3 < t <4
t4=np.linspace(3,4,20)
z=np.zeros(20)

#x(t)
x=np.concatenate((x3,x1,x2,z),
    axis = 0)

t = np.concatenate((t3,t1,t2,t4),
    axis = 0)

#x(-t)
xflip = np.fliplr([x])[0]

#Plotting
plt.plot(t,x, label='$x(t)$')
```

```
plt.plot(t,xflip, label='$x(-t)$')

plt.grid()
plt.xlabel('$t$')
plt.ylabel('$x(t)$')
plt.legend()
plt.axis('equal')
##Ignore the following command
plt.savefig('../figs/4b.eps')
plt.show()
```

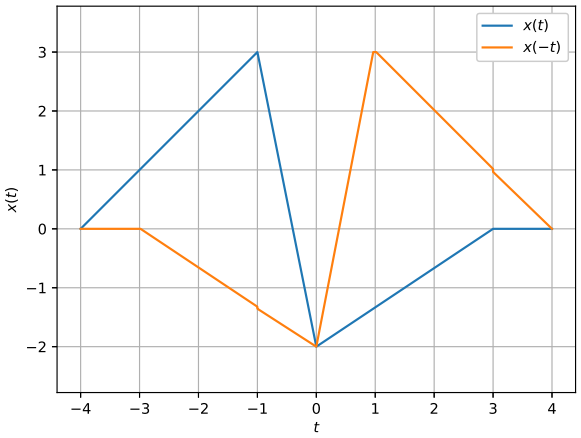

Fig. 7

Problem 8. Sketch

$$x(t) = \begin{cases} 3(t+4) & -4 \le t \le -3 \\ -5t-12 & -3 < t < -2 \\ 3t+4 & -2 \le t \le -1 \\ -t & -1 < t < 1 \\ 3t-4 & 1 \le t \le 2 \\ -5t+12 & 2 < t < 3 \\ 3(t-4) & 3 \le t \le 4 \\ 0 & \text{otherwise} \end{cases} \tag{8.1}$$

and find out if its even or odd.

Solution: The following code yields Fig. 8. As we can see, $x(t) = -x(-t)$ and the function is odd.

```
import numpy as np
import matplotlib.pyplot as plt

#-4 < t < -3
t7=np.linspace(-4,-3,25)
x7=(t7+4)*3

#-3 < t < -2
t5=np.linspace(-3,-2,25)
x5=(-5*t5)-12

# -2 < t < -1
t4=np.linspace(-2,-1,25)
x4=3*(t4)+4

#-1 < t < 1
t1=np.linspace(-1,1,25)
x1=-t1

#1 < t < 2
t2=np.linspace(1,2,25)
x2=3*(t2)-4

#2 < t < 3
t3=np.linspace(2,3,25)
x3=(-5*t3)+12

#3 < t < 4
t6=np.linspace(3,4,25)
x6=(t6-4)*3

#x(t)
x=np.concatenate((x7,x5,x4,x1,x2,
    x3,x6), axis = 0)

t = np.concatenate((t7,t5,t4,t1,t2
    ,t3,t6), axis = 0)

#x(-t)
xflip =np.fliplr([x])[0]

#Plotting
plt.plot(t,x, label='$x(t)$')
plt.plot(t,xflip,'o', mfc='none',
    label='$x(-t)$')

plt.grid()
plt.xlabel('$t$')
plt.ylabel('$x(t)$ and $x(-t)$')
plt.legend()
##Ignore the following command
plt.savefig('../figs/4c.eps')
plt.show()
```

Problems 9-13 are related.

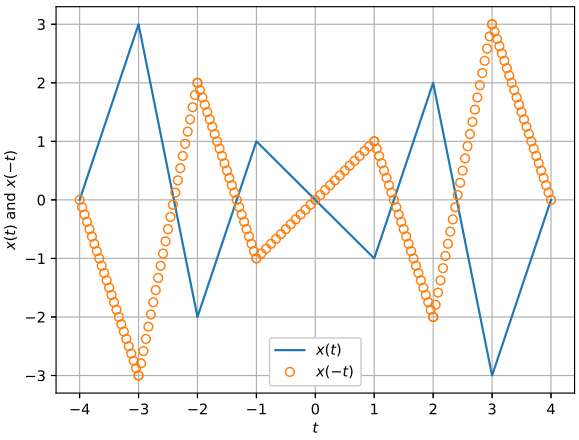

Fig. 8

Problem 9. Sketch

$$x(t) = \begin{cases} t+4 & -4 \le t \le -2 \\ t-4 & 2 \le t \le 4 \\ 0 & \text{otherwise} \end{cases} \tag{9.1}$$

Solution: The following code yields Fig. 9

```
import numpy as np
import matplotlib.pyplot as plt


t1=np.linspace(-6,-4,10)
t2=np.linspace(-4,-2,10)
t3=np.linspace(-2,2,10)
t4=np.linspace(2,4,10)
t5=np.linspace(4,6,10)

x1=t1*0
x2=t2+4
x3=t3*0
x4=t4-4
x5=t5*0

#x(t)
x=np.concatenate((x1,x2,x3,x4,x5),
    axis=0)

t=np.concatenate((t1,t2,t3,t4,t5),
    axis=0)

plt.plot(t,x)

plt.xlabel('t')
plt.ylabel('x(t)')
plt.grid()
#Ignore the following command
plt.savefig('../figs/8.eps')
plt.show()
```

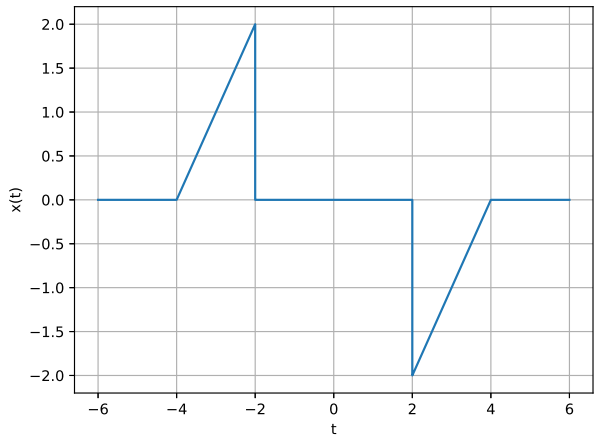

Fig. 9

Problem 10. Sketch $x(t+1)$

Solution: The following code yields Fig. 10

```
import numpy as np
import matplotlib.pyplot as plt
from scipy.ndimage.interpolation
    import shift

t1=np.linspace(-6,-4,40)
t2=np.linspace(-4,-2,40)
t3=np.linspace(-2,2,80)
t4=np.linspace(2,4,40)
t5=np.linspace(4,6,40)

x2=t2+4
x3=t3*0
x4=t4-4
x1=t1*0

x=np.concatenate((x1,x2,x3,x4,x1),
    axis=0)

t=np.concatenate((t1,t2,t3,t4,t5),
    axis=0)

# 0-1 x(t) has 10 samples i.e., x(
    t+1)=x(n-20)
```

```
andig = 20
anshift = -1

x_t=shift(x, anshift*andig, cval=0)

plt.plot(t,x,label='x(t)')
plt.plot(t,x_t,label='x(t+1)')
plt.xlabel('t')
plt.ylabel('$x(t)$ and $x(t+1)$')
plt.axis([-6,6,-3,3])
plt.grid()
plt.legend()
#Ignore the following command
plt.savefig('../figs/8a.eps')
plt.show()
```

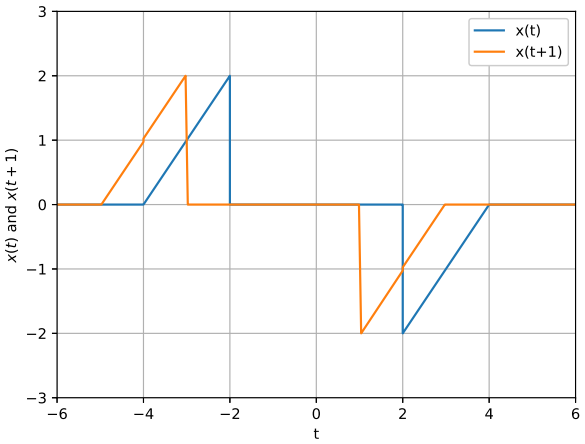

Fig. 10

Problem 11. Sketch $5x\left(\frac{t}{3}\right)$

Problem 12. Sketch $2x(t-2)$

Problem 13. Sketch $x(t) - x(-t)$.

Problems 14-16 are related.

Problem 14. Let $x(t) = e^{-t}$ and $y(t) = x(t)u(t)$. Sketch $x(t)$ and $y(t)$.

Problem 15. Sketch $x_1(t) = x(t-2)$ and $y_1(t)$, where $y_1(t)$ is the output when $x_1(t)$ is the input to the system.

Problem 16. Sketch $y(t-2)$ and $y_1(t)$ in the same graph. Is the system time invariant?

Problems 17-18 are related.

Problem 17. If $x(t) = u(t)$, sketch

$$y(t) = \sum_{m=-1}^{2} mx(t-m) \tag{17.1}$$

Problem 18. Sketch $h(t)$ for the previous problem. Is the system causal?

Problems 19-23 are related.

Problem 19. Sketch

$$x(k) = \left\{-1, -1, \underset{\uparrow}{-1}, 1, -1, 1, 1, 1\right\} \tag{19.1}$$

and

$$h(k) = \left\{\underset{\uparrow}{0}, -1, 1\right\} \tag{19.2}$$

Problem 20. Sketch $h(-k)$ and $x(k)h(n-k)$ for $n = -2, -1, \ldots, 7$.

Problem 21. Sketch $y(n) = \sum_k x(k)h(n-k)$ for $n = -2, -1, \ldots, 7$.

Problem 22. Run the following code and compare with the result of the previous problem.

```
import numpy as np
import matplotlib.pyplot as plt
from scipy.ndimage.interpolation
    import shift

#x(n-2)
x=[-1,-1,-1,1,-1,1,1,1]
#h(n)
h=[0,-1,1]
#y(n-2)
yns=np.convolve(x,h)
n = np.linspace(-2,7,10)
plt.stem(n,yns)
#plt.stem(yns)
plt.xlabel('n')
plt.ylabel('y(n)=x(n)*h(n)')
plt.grid()

plt.show()
```

Problem 23. Sketch $h(n) * h(-n)$.